Equivalent Circuit Consideration of Frequency-Shift-Type Acceleration Sensor

周波数変化型加速度センサの等価回路考察

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1. Introduction

Recently, a highly sensitive acceleration sensor suitable for MEMS structure is required for attitude control of moving objects such as vehicles and robots.¹⁾ As such a sensor, a frequency-shifttype acceleration sensor utilizing the resonance frequency of the bending vibrator by the axial force has been proposed.^{1, 2)} Although multi-axialization and combination with an angular velocity sensor are studied³⁾, an electrical equivalent circuit for estimating various characteristics of the frequencyshift-type sensor has not been derived.

Therefore, the equivalent circuit representation for the piezoelectrically driven sensor model is investigated here. The equation for estimating the resonance frequency of the vibrator approximately is derived. Moreover, acceleration dependence of the equivalent circuit constants is analyzed by the finite element method, and compared with the measured one.

2. Structure and Mode of Vibration

Fig. 1 shows the basic structure of the acceleration sensor with a bending vibrator. The sensor is made of stainless steel (SUS304), and its vibrator is piezoelectrically driven. The frequency of the vibrator is shifted by the axial force due to the acceleration α applied to the mass from the x



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axis direction. Therefore, the acceleration can be estimated from the frequency shift. **Fig. 2** shows the out-of-plane vibration modes of the vibraor.

3. Equivalent Circuit Consideration

3.1 Approximate estimation of resonance frequency

In the case of a usual bending vibrator with a uniform rectangular cross-section, the n-th mode resonance frequency f_n considering the influence of the axial force is given by the following equation.⁴⁾

$$f_n = \frac{\alpha_n^2}{2\pi\ell_{en}^2} \sqrt{\frac{EI}{\rho A}} \tag{1}$$

Where E, ρ , A and I are Young's modulus, the density, the cross-sectional area and the moment of inertia of area, also ℓ_{en} and α_n are the length of the vibrator and the frequency constant of n-th mode, respectively. The constant α_n is given as a function of the axial force F. The constants, α_{01} and α_{02} of the 1st and 2nd mode become well-known values of 4.7300 and 7.8532, respectively when F=0. The characteristics of $f_n - \ell_{en}/\ell_n$ are calculated by eq. (1) as shown in Fig. 3, where ℓ_n is the total length of the bending vibrator of the sensor. The resonance frequencies f_{01} and f_{02} of the vibrator are also shown in the figure. The thickness of the vibrator is 0.2mm. From the figure, the value of ℓ_{en}/ℓ_n for the 1st or 2nd mode is determined as 0.79 or 0.77, respectively. Accordingly, the effective lengths ℓ_{en} for realizing the frequencies f_{01} and f_{02} are



Fig. 3 Characteristics of $f_{0n} - \ell_{en}/\ell_n$.

estimated, the frequency shift by the axial force can be easily analyzed by using eq. (1).

3.2 Electrical equivalent circuit

Fig. 4 shows the electrical equivalent circuit of the bending vibrator. The values of the circuit constants analyzed by the finite element method and the measured values are listed in **Table I**. From the table, it became clear that the analyzed values agree with the measured ones.



Fig. 4 Equivalent circuit of vibrator.

	1st mode (n=1)		2nd mode (n=2)	
	Measured	Analyzed	Measured	Analyzed
f_0 (Hz)	1685.7	1695.7	4562.5	4559.0
C_d (pF)	494.7	492.0	747.8	766.0
$C_{\rm n}$ (pF)	1.262	1.254	1.684	1.689
L_{n} (H)	7082.8	7026.8	720.48	721.50

 Table I
 Resonance frequency and equivalent circuit constants of sensor

3.3 Acceleration dependence of circuit constants

Fig. 5 shows the relationship between the acceleration α changed within the range of ± 1 G and the resonance frequency shift ratio of $\Delta f_{x}/f_{0}$ analyzed by the finite element method. The measured values are also shown in the figure. The analyzed values are almost the same as the measured ones.⁴⁾ Moreover, relationship between α and L_{n} are shown in **Figs. 6** and 7 respectively. The changes in the values of C_{n} and L_{n} were very small. It was confirmed that the analyzed values agree with the measured ones.

4. Conclusions

The resonance frequency, the equivalent circuit constants and their acceleration dependence of the piezoelectrically driven frequency-shift-type acceleration sensor were analyzed by the finite element method. As a result, it was confirmed that the analyzed values agree with the measured ones. As a future work, a simplified approach to estimate the resonance frequency and the equivalent circuit constants taking the influence of the axial force into consideration should be investigated.

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